

## Evaluation of Numerical Dissipation Sensitivity Using IDDES

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**Abstract:** Improved-Delayed Detached Eddy Simulation (IDDES) method based on two equation  $k$ - $\omega$ -SST (shear layer transport) model is applied to simulate the decay of homogeneous isotropic turbulence (DHIT) and massive separation flows past tandem cylinders (TC) flows with space of 3.7 diameters (D). Fourth order Jameson-type central scheme (C4) and high order symmetric total variation diminishing (STVD) scheme with adaptive dissipation are formulated by introducing a function ( $\phi$ ) dependent on the turbulent flow. The numerical dissipation sensitivity is evaluated by changing the threshold of the function ( $\phi_{\min}$ ). For the DHIT case, the large  $\phi_{\min}$  suppresses the cascade of the energy and the very small  $\phi_{\min}$  can match the measurements well; both C4 and STVD schemes have the same tendency. For the TC case, the primary differences of computations are caused by the fundamental schemes, while  $\phi_{\min}$  has a relatively weak influence. Due to a small background artificial viscosity coefficient  $k^{(4)}$  of 1/100 in C4 scheme, undesired small  $\phi$  ( $<1$ ) region before the front cylinder is presented, which leads to the appearance of the numerical noise in the near-field around TC; The performance of S6WENO5 is better and anticipant. The shear layer instability happens a little more upstream and structures are smaller with smaller  $\phi_{\min}$ .

*Keywords:* IDDES, DHIT, TC, adaptive dissipation, threshold of the function  $\phi_{\min}$

## 1 Introduction

Detached eddy simulation (DES) was originally developed to accurately simulate the massively separated flows (Spalart et al., 1997). Due to its high accuracy and efficiency, it was widely used and obtained further improvements. To avoid the undesired transition from RANS (Reynolds-averaged Navier-Stokes) to LES (large eddy simulation) in the attached boundary layer induced by the locally clustered grids, Menter et al. (2003) and Spalart et al. (2006) proposed DDES based on two-equation SST model and one-equation model SA model, respectively. To cure the log-layer mismatch problem, Shur et al. (2008) proposed IDDES, which combines the advantage of DDES and wall-modeled LES (WMLES). In our previous work (Xiao et al., 2011), the performances of three advanced DES methods, such as DDES-2003, 2006 and IDDES, were compared through simulating the massively separated flows past TC case. It's found that the major difference between DDES-2003 and DDES-2006 is the shielding function, which leads to the different range of RANS region. Due to the WMLES mode, IDDES performs better for the shear layer instability and root mean square of pressure coefficient. Then, IDDES is chosen as the turbulence simulation model to predict the

extremely unsteady and massively separated flow past TC in this article. In our previous work about the massive separation around rudimentary landing gear [Xiao et al, 2012], IDDES performs better than DDES on the surface flow patterns, such as the range of horseshoe vortex, secondary separation, and so on.

The natural choice for the numerical scheme of LES and LES/RANS hybrid approaches is the central-type schemes. However, the purely central schemes often suffer from the numerical instability, because the grids near the wall and in the irrotational region are not fine enough to fully resolve the turbulence. Therefore, in these regions, the appropriate numerical dissipation is also required. More and more people have realized the deficiency of the upwind discretization scheme and made very good efforts in eliminating the negative effect of the numerical dissipation to provide accurate results. Three types of efforts can be classified as: (1) increasing the discretization order of the scheme; (2) reducing the numerical dissipation; (3) both.

Bui (1999) directly reduced the dissipation of upwind Roe scheme with 3<sup>rd</sup> monotone upstream-central schemes for conservation laws (MUSCL) interpolation by multiplying a small constant, ranging from 0.03 to 0.05, to calculate the fully developed turbulence in a square duct with LES. Qin and Xia (2008) reduced the numerical dissipation of Roe scheme in the same way to predict the synthetic jet flow. To obtain the balance of numerical accuracy and stability, the relatively large constant is taken as 0.4. This approach is very simple and easily to implement, but it is too empirical and lacks physics.

The combination of the central and upwind scheme (Strelets, 2001; Mockett, 2009) was smartly designed to accurately predict the turbulence. This upwind/central hybrid scheme functions acts as an effectively central scheme in the separated regions where DES is operating in an LES mode, and as an upwind-biased scheme near the wall (RANS mode) and in the outer irrotational regions.

In our previous work, Xiao et al. (2012) investigated the numerical dissipation effect on the massively separated flows past TC using original upwind Roe scheme with MUSCL interpolation, S6WENO5 (6<sup>th</sup> order symmetric scheme with 5<sup>th</sup> order weighted essential non-oscillating interpolation) scheme with 12% dissipation and S6WENO5 scheme with adaptive dissipation (Strelets, 2001), coupled with DDES methods. It's found that the original Roe scheme is too dissipative. It over-predicts the root mean square of pressure coefficients and greatly suppresses the generation of the small-scale structures. S6WENO5 scheme with 12% dissipation performs much better than the original Roe scheme. Unfortunately, it is too empirical. S6WENO5 scheme with adaptive dissipation performs best and it can well predict the mean and instantaneous flows.

Spalart et al. (2012) investigated the unsteady flow and noise from the landing gear using 4<sup>th</sup> central and 3<sup>rd</sup> upwind Roe hybrid scheme with three thresholds of adaptive function ( $\phi_{\min}$ ) of 0, 0.2 and 0.4, respectively. When the more upwind-biased differencing is used, the small-scale contents are greatly reduced. The performance is greatly affected by different  $\phi_{\min}$ , which is highly undesirable.

In this article, the threshold of adaptive function ( $\phi_{\min}$ ) of numerical dissipation is evaluated based on two schemes, 4<sup>th</sup> order Jameson type central (C4) scheme only with 4<sup>th</sup> artificial viscosity and S6WENO5 scheme. To obtain reasonable results, the values of  $\phi_{\min}$  are less than 0.1. At the same time, the effects of the fundamental schemes on the flow features, such as turbulence energy cascade, shear layer instability, pressure fluctuations, turbulent kinetic energy (TKE) and so on, are explored through comparing with the available measurements.

## 2 Spatical Schemes and Adaptive Dissipation

The in-house code of UNITS (*Un*steady *Nav*ier-*St*okes solver), which is in a cell-centered finite-volume formulation based on multi-block structured grids, is applied to evaluate the numerical dissipation sensitivity. A modified fully implicit LU-SGS with Newton-like sub-iteration in pseudo time is taken as the time marching method when solving the N-S and the turbulence model equations. The approach is a parallel algorithm using domain-decomposition and message-passing-interface strategies for the platform on computer clusters.

In this paper, two high order schemes are used. One is the Jameson-type (1981) C4 scheme and the other is S6WENO5 scheme (2002). The reason for choosing the STVD scheme is that this algorithm allows the independent control of the dispersion and dissipation errors in the solution.

According to our experience, the original Jameson-type central and STVD scheme are often dissipative and they can greatly suppress the generation of small structures. Then, their dissipation should be effectively decreased in the separation region. As was analyzed before, the numerical dissipation should be large enough near the wall and in the irrotational region where the grid are relatively too coarse to accurately resolve the turbulence. The adaptive function, dependent on the flow and grid scale, can be introduced in the convective terms of N-S equations.

The invicid flux of N-S equations can be written as:

$$F_{i+1/2} = f_{i+1/2} + D_{i+1/2} \quad (1)$$

In equation (1),  $f_{i+1/2}$  is the symmetric or central flux and  $D_{i+1/2}$  is the pure dissipation.

For the S6WENO5 scheme,

$$f_{i+1/2} = (F_{i-2} - 8F_{i-1} + 37F_i + 37F_{i+1} - 8F_{i+2} + F_{i+3})/60 \quad (2)$$

$$D_{i+1/2} = -0.5 \times \phi \times \left[ \tilde{A}_{\text{inv}} \left| (q^R - q^L) \right| \right]_{i+1/2} \quad (3)$$

where  $q^R$  and  $q^L$  are the original variables on the right and left side of the interface. In Equation (2), the symmetric scheme is 6<sup>th</sup> order; in equation (3), the original variables are obtained through 5<sup>th</sup> WENO interpolation.

For the C4 scheme, only the fourth artificial viscosity remains due to low speed flow. The symmetric flux and dissipation are given as:

$$f_{i+1/2} = (-F_{i-1} + 7F_i + 7F_{i+1} - F_{i+2})/12 \quad (4)$$

$$D_{i+1/2} = D_{i+1/2}^{(4)} = -\lambda_{i+1/2} \epsilon_{i+1/2}^{(4)} (q_{i+2} - 3q_{i+1} + 3q_i - q_{i-1}), \epsilon_{i+1/2}^{(4)} = \text{Max}(0, \phi \times k^{(4)}) \quad (5)$$

where 4<sup>th</sup> background artificial viscosity coefficients  $k^{(4)}$  is taken as 1/100;  $\lambda$  is the spectral radius and  $q$  are the primary variables.

In equation (3) and (5),  $\phi$  is an adaptive function dependent on the turbulence flow and grid scale. It can be written as:

$$\phi = \phi_{\text{max}} \tanh(A^{\text{CH1}}) \quad (6)$$

where  $\phi_{\text{max}}$  is always taken as 1. It means that  $\phi$  theoretically ranges from 0 to 1. The definition of  $\phi$  can be found in our previous work (Xiao et al., 2012) or some other references (Strelets, 2001; Mockett, 2009 and Spalart, 2012). Then,  $\phi$  is designed to be 0 in the separation regions and to become 1 near wall and in irrotational regions. When it is equal to 0, the S6WENO5 scheme becomes the sixth order symmetric scheme without dissipation and C4 scheme is a pure central scheme without any artificial viscosity. When it is equal to 1, it returns to the original scheme.

As we know, high order purely central schemes always suffer from numerical difficulty, and then we should set a threshold of the adaptive function,  $\phi_{\text{min}}$ . Then the final adaptive function can be written as:

$$\phi = \max(\phi, \phi_{\text{min}}) \quad (7)$$

where  $\phi_{\text{min}}$  is a constant, which can be taken as 0.01, 0.1, even 1. To ensure numerical accuracy, it is hoped to be as small as possible.

### 3 Turbulence Simulation Methods

Differing from the original DES (Spalart et al., 1997), DDES (Spalart et al, 2006) and IDDES (Shur et al., 2008), the background turbulence model in this article is not taken as one-equation S-A model (Spalart, 1992), but two-equation SST model (Menter, 1994). IDDES methods could be constructed by modifying the destruction term of the TKE equation and by introducing a length scale,  $L_{\text{hybrid}}$

$$\frac{\partial(\rho k)}{\partial t} + \frac{\partial(\rho u_j k)}{\partial x_j} = \frac{\partial}{\partial x_j} \left( \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right) + \tau_{ij} S_{ij} - \frac{\rho k^{3/2}}{L_{\text{hybrid}}} \quad (8)$$

For IDDES, the length scale of  $L_{\text{hybrid}}$  can be written as

$$L_{\text{hybrid}} = L_{\text{IDDES}} = \tilde{f}_d (1 + f_e) \times L_{\text{RANS}} + (1 - \tilde{f}_d) \times L_{\text{LES}} \quad (9)$$

where the length scale of  $L_{\text{RANS}}$  is defined as  $k^{0.5}/(\beta^* \omega)$  and  $L_{\text{LES}}$  is defined as  $C_{\text{DES}} \times \Delta$ , where  $\Delta = \max(\Delta x, \Delta y, \Delta z)$ . For IDDES, the grid scale is redefined as  $\Delta = \min[\max(C_w \Delta_{\text{max}}; C_w D_w; \Delta_{\text{min}})]$ ;

$\Delta_{\max}$ ]. When  $f_e$  is equal to 0,  $L_{IDDES} = \tilde{f}_d \times L_{RANS} + (1 - \tilde{f}_d) \times L_{LES}$  and it acts in DDES mode. Function  $\tilde{f}_d$  is defined as  $\max[(1 - f_{dt}), f_B]$ . It is determined by both the geometry part  $f_B$  and the flow part  $(1 - f_{dt})$ . When  $f_e$  is larger than zero and  $\tilde{f}_d$  is equal to  $f_B$ ,  $L_{IDDES} = L_{WMLES} = f_B(1 + f_e) \times L_{RANS} + (1 - f_B) \times L_{LES}$ , and it acts in WMLES mode.

## 4 Results and Discussions

The turbulence modeling method is the IDDES based on SST model. The constant  $C_{DES}$  has been calibrated using UNITS (Xiao et al., 2012). In this paper, we focus on evaluating the effects of threshold of adaptive function ( $\phi_{\min}$ ) on the flow features, such as energy cascade, mean pressure, mean velocity, instantaneous shear layer instability, pressure fluctuation, and so on.

### 4.1 Decay of Homogenous Isotropic Turbulence

DHIT is a fundamental test case for the development of turbulence modeling and/or numerical techniques as it is the simplest realization of the turbulent flow. On the one hand, the capability and quality of LES part in IDDES can be evaluated. On the other hand, the empirical parameter  $C_{DES}$  can be recalibrated. At the same time, the dissipation level of the present in-house CFD code can be evaluated. To obtain more resolved turbulence, the dissipation level of numerical scheme should be reduced effectively wherever LES is activated.

The computational domain contains  $32^3$  uniform cells. The computation of DHIT is established in a cubic domain with periodic boundary conditions in all three directions to reflect the homogeneity of the flow. The temporal scheme is the implicit LU-SGS method with very small non-dimensional time step (0.0001 here).

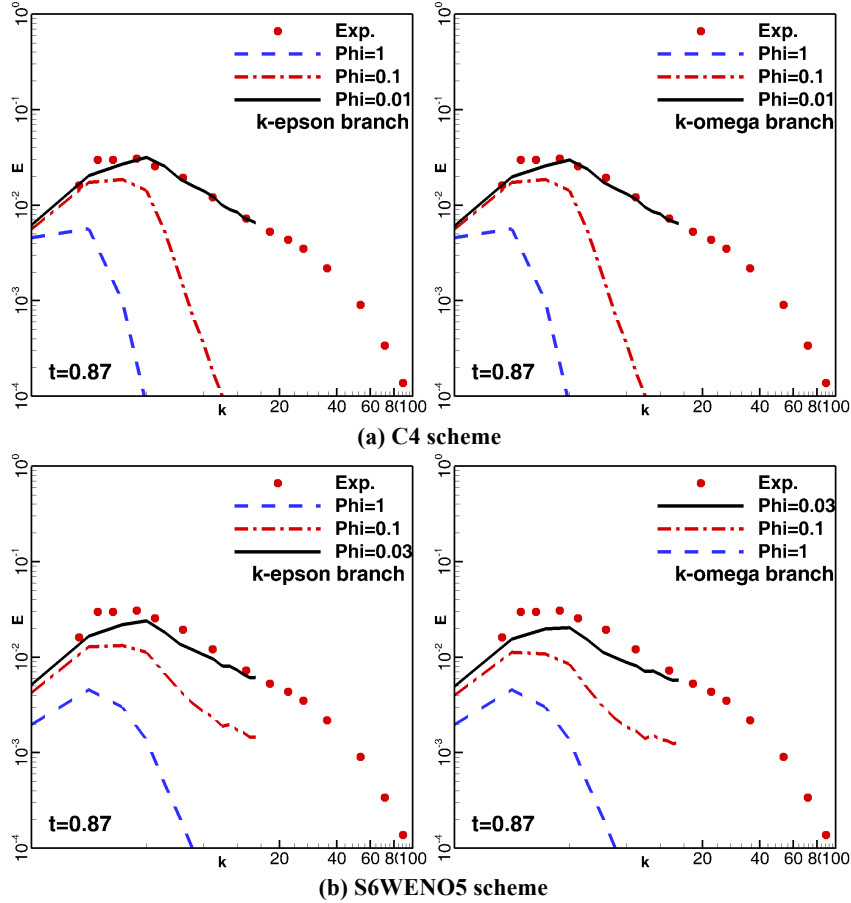


Figure 1: The effects of  $\phi_{\min}$  on energy spectra of DHIT.

Like Menter's SST model, IDDES based on SST model also contains  $k-\omega$  and  $k-\epsilon$  branches. For the



DHIT, the  $k$ - $\varepsilon$  branch is more important because there is no wall in the computational domain. Figure 1 presents the energy cascade by C4 and S6WENO5 schemes, respectively. For the DHIT case,  $\phi$  is a constant and it is equal to  $\phi_{\min}$ . When  $\phi$  is equal to 1, the spatial scheme is the original C4 and S6WENO5 schemes. When  $\phi$  is equal to 0, the spatial scheme becomes the 4<sup>th</sup> or 6<sup>th</sup> order central scheme.

- (1) For the C4 scheme: The original scheme, where  $\phi=1$  and  $k^{(4)}=1/100$ , greatly under-predicts the energy cascade for the all wave numbers. When  $\phi$  is reduced to 0.1, where  $k^{(4)}=1/1000$ , it only under-predicts the energy at high-wave numbers. When  $\phi$  is equal to 0.01, where  $k^{(4)}$  is equal to 1/10000, it can well predict the energy at both the low- and high-wave numbers. This indicates that 1/10000 of  $k^{(4)}$  is an appropriate parameter of  $\phi_{\min}$ . The performances of  $k$ - $\varepsilon$  and  $k$ - $\omega$  parts differ little.
- (2) For the S6WENO5 scheme: The original STVD scheme, where  $\phi=1$ , greatly under-predicts the energy cascade for all the wave numbers. When  $\phi$  is reduced to 0.1, it also under-predicts the energy, especially at high wave number. When  $\phi$  is taken as 0.03, the scheme can well predict the energy at both low and high wave numbers. It indicates that 0.03 is a good choice of  $\phi_{\min}$  when S6WENO5 scheme is applied. The energy of  $k$ - $\varepsilon$  part is a little larger than that of  $k$ - $\omega$  part using the same  $\phi$ .

In fact, the computations for the complex unsteady flows based on the non-uniform grids often suffer numerical difficulties if the  $\phi_{\min}$  value recommended by DHIT case is applied. The actual  $\phi_{\min}$  is usually adjusted to a little larger value.

## 4.2 Tandem Cylinders

The TC case studied here is the one investigated experimentally by Jenkins et al. (2005, 2006 and 2009). It is known to associate with complex flow phenomena, like the transition, separation of turbulent boundary layer, shear layer instability, the interaction of unsteady wake of the front cylinder with the downstream one and unsteady massively separated flow between the cylinders and in the wake of the rear cylinder, and so on. Thus, it is a standard test case in the European 7<sup>th</sup> Framework project Advanced Turbulence Simulation for Aerodynamic Application Challenges (ATAAC) (2009-2012) and AIAA Workshop on Benchmark problems for Airframe Noise Computations (BANC I and II, 2010, 2012).

The diameters ( $D$ ) of the two cylinders are the same. The spacing  $L$  is  $3.7D$ . The velocity of freestream is 44m/s, the Reynolds number based on  $D$  is  $1.66 \times 10^5$  and the angle of attack is 0 degree. In order to resolve the small-scale structures, the two-dimensional grids between the cylinders are almost isotropic (about 0.01-0.02  $D$ ). The spanwise domain is taken as  $3D$  with equal intervals of 0.02 $D$ . The overall cells are 12.4 million for the three-dimensional computational domain. The non-dimensional time step is 0.01.

In the present simulations, no-slip conditions are imposed on the cylinders' walls. Symmetric conditions are applied on the lateral sides of the wind-tunnel test-section and periodic conditions are taken in the spanwise direction. At inflow and outflow boundaries, the one-dimensional Riemann characteristic analysis is employed to construct a non-reflection boundary condition. "Ghost cells" are employed to treat all kinds of boundary conditions including the boundaries of the adjacent zonal domains.

As mentioned before, the computations usually suffer numerical difficulties if  $\phi_{\min}$  is too small, especially when using the C4 scheme. To ensure the computations on going,  $\phi_{\min}$  in C4 scheme are taken as 0.05 and 0.1. For S6WENO5 scheme,  $\phi_{\min}$  is taken as 0.03 and 0.1.

### 4.2.1 Histories of Drag Coefficient ( $C_d$ )

Figure 2 presents the histories of  $C_d$  on the front and rear cylinders by C4 and S6WENO5 with different  $\phi_{\min}$ . From it, the  $C_d$  fluctuation amplitude of the front cylinder is significantly smaller than that of the rear one. It means that the flow past the front cylinder seems relatively "quiet". This feature is easily understood as the front cylinder encounters weaker disturbances of the free-stream than the rear one, which is in the extremely unsteady wake detached from the front cylinder.

After averaging the instantaneous drag coefficients ( $C_d$ ), the mean  $C_d$  coefficients are listed in Table 1. The difference is mainly caused by the fundamental schemes and different  $\phi_{\min}$  have a relatively weak influence.

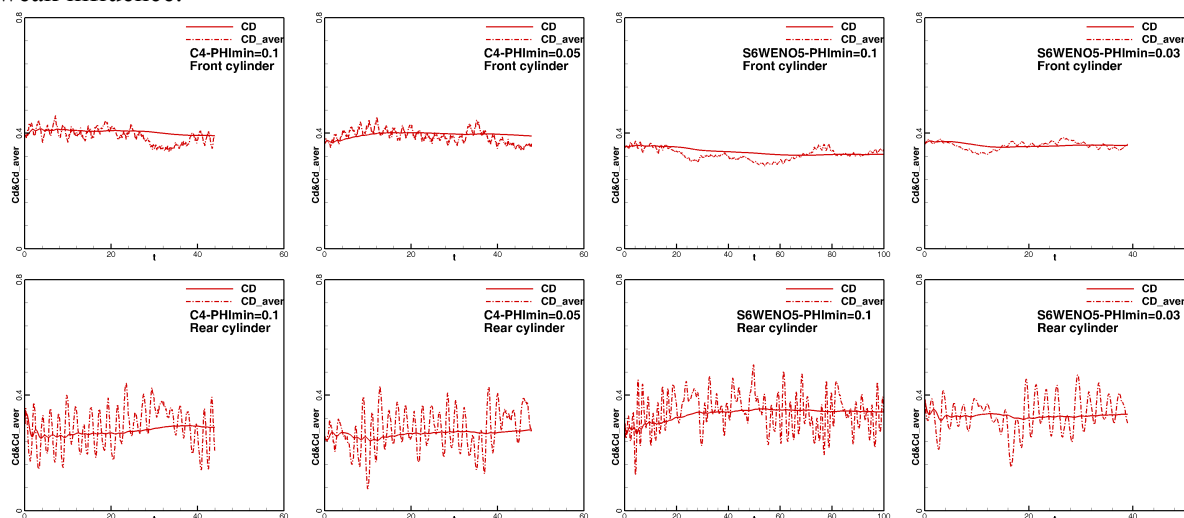


Figure 2. The histories of drag coefficients

Schemes and $\phi_{\min}$		Averaging time $T$	Averaged $C_D$ of Front cylinder	Averaged $C_D$ of Rear cylinder
S6WENO5	$\phi_{\min}=0.1$	100	0.441	0.455
	$\phi_{\min}=0.03$	41	0.476	0.437
C4	$\phi_{\min}=0.1$	50	0.522	0.385
	$\phi_{\min}=0.05$	45	0.520	0.373

Table 1 The comparisons of  $C_d$  using different schemes and  $\phi_{\min}$

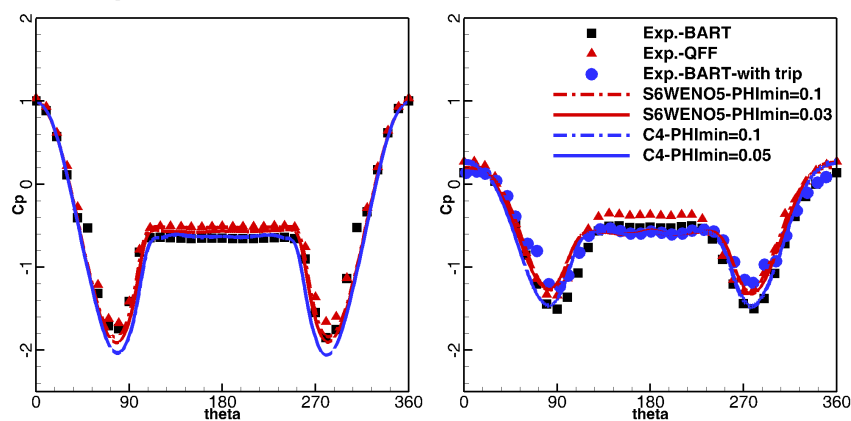
#### 4.2.2 Effects on Mean Pressure and Root Mean Square Pressure

Figure 3 presents the comparisons of  $C_p$  and  $C_{p,rms}$  by C4 and S6WENO5 schemes with different  $\phi_{\min}$ . The primary difference is not caused by  $\phi_{\min}$ , but by the fundamental schemes.

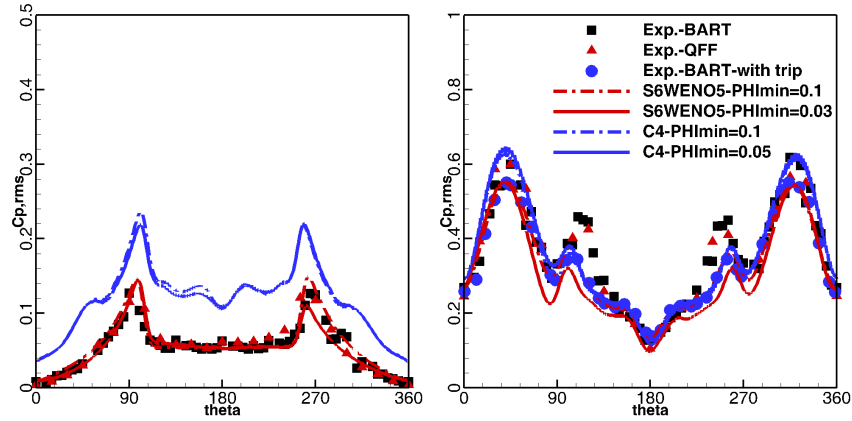
Both C4 and S6WENO5 can well predict the mean  $C_p$  on the two cylinders and they differ from each other slightly. C4 presents a little larger suction peaks near 90 and 270 degrees than those of S6WENO5.

After comparing the  $C_{p,rms}$ ,

- (1) On the front cylinder: C4 obviously over-predicts the  $C_{p,rms}$  than those of the experiments and S6WENO5. S6WENO5 with  $\phi_{\min}$  of 0.03 and 0.1 well match the measurements. It seems that S6WENO5 with  $\phi_{\min}$  of 0.1 performs better than that with  $\phi_{\min}$  of 0.03. The latter  $\phi_{\min}$  presents a little smaller  $C_{p,rms}$  at about 270 degrees than the measurements.



(a) Mean  $C_p$  on the cylinders



(b)  $C_{p,rms}$  on the cylinders

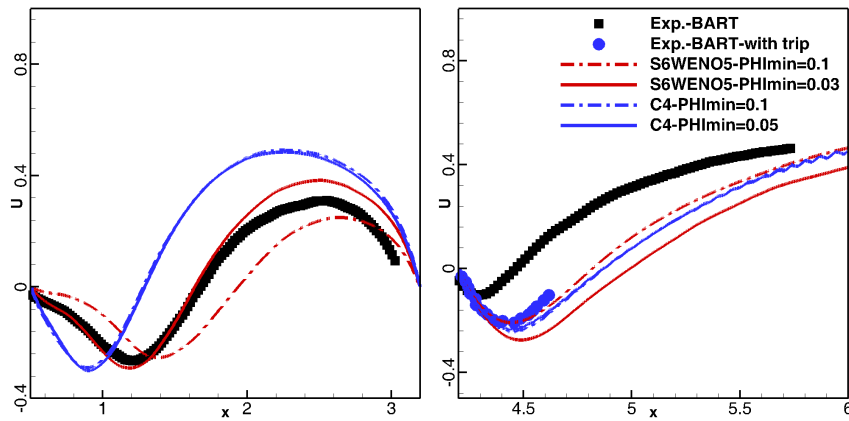
Figure 3. Comparisons of  $C_p$  and  $C_{p,rms}$

- (2) On the rear cylinder: Both C4 and S6WENO5 can well match the measurements, although C4 presents a little larger  $C_{p,rms}$  than those of S6WENO5. In S6WENO5 scheme, the large  $\phi_{min}$  performs better than the small one.

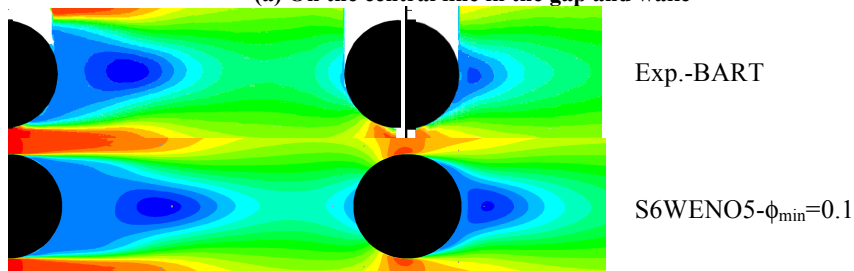
#### 4.2.3 Effects on Mean Velocity in Space

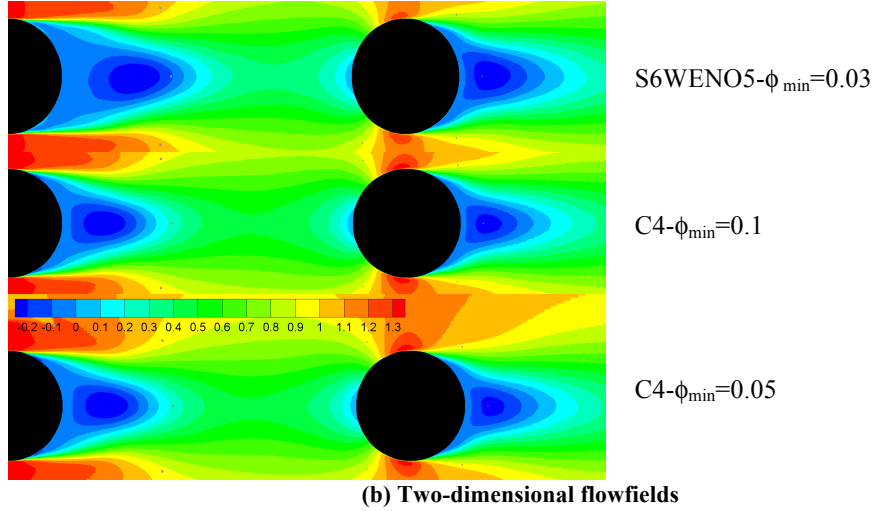
Figure 4 presents the comparisons of the mean streamwise velocity by C4 and S6WENO5 with different  $\phi_{min}$ . All the schemes over-predict the recirculation behind the rear cylinder, even comparing with the measurements with trip on the windward surface of the rear cylinder, whose recirculation looks much larger than that without trip.

- (1) C4 schemes with  $\phi_{min}$  of 0.1 and 0.05 differ from each other slightly. Both of them under-predict the recirculation in the gap region and over-predict the recirculation in the wake.
- (2) S6WENO5 scheme performs better than C4. S6WENO with  $\phi_{min}$  of 0.03 well matches the measurements in the gap region, while it over-predicts the recirculation in the wake. S6WENO5 with  $\phi_{min}$  of 0.1 also over-predicts the recirculation in the gap region but it well matches the recirculation in measurements of BART with trip. Here, larger  $\phi_{min}$  leads to a larger recirculation in the gap region.



(a) On the central line in the gap and wake





(b) Two-dimensional flowfields  
**Figure 4 Comparisons on the mean streamwise velocity**

#### 4.2.3 Effects on TKE in Space

Figure 5 presents the comparisons of the mean TKE by C4 and S6WENO5 with different  $\phi_{\min}$ .

Like the streamwise velocity, C4 with different values of  $\phi_{\min}$  perform almost the same.

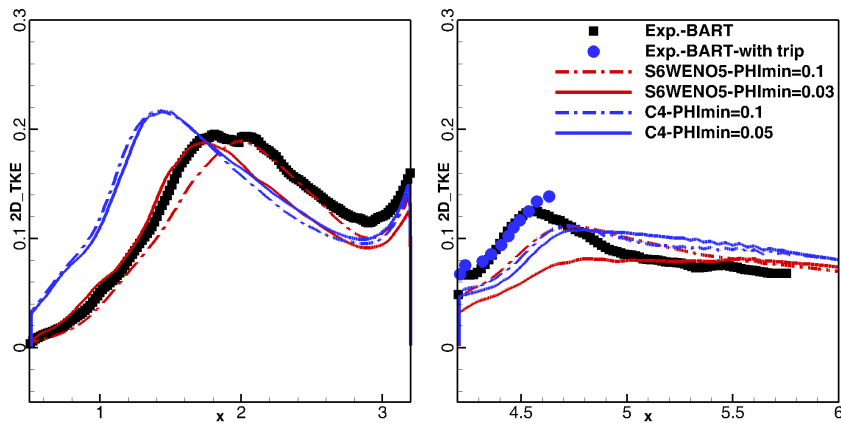
- (1) In the gap region, due to small recirculation, C4 over-predicts the TKE before  $x/D=1.9$ , while it under-predicts the TKE after  $x/D=1.9$ . In the wake after the rear cylinder, C4 under-predicts the TKE.
- (2) C4 scheme with  $\phi_{\min}$  of 0.1 predicts a little larger TKE before the peaks and smaller TKE after the peaks than those by C4 with  $\phi_{\min}$  of 0.05.

S6WENO5 scheme with two values of  $\phi_{\min}$  presents a relatively distinguished difference.

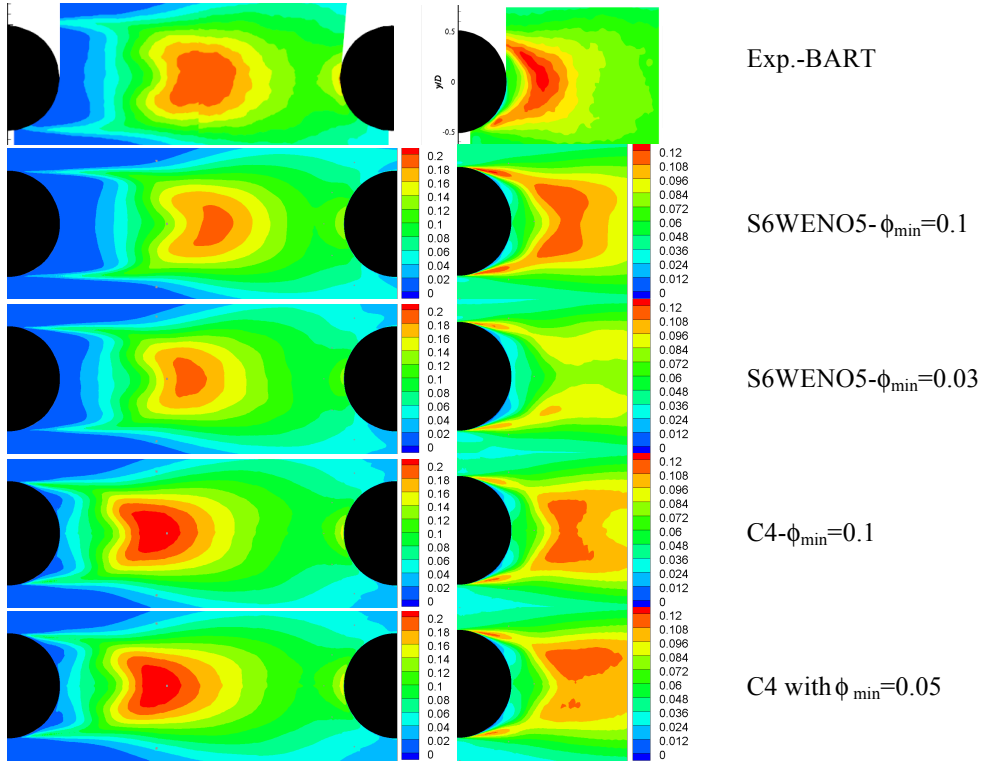
- (1) In the gap region, S6WENO5 with  $\phi_{\min}$  of 0.03 well matches the measurements before  $x/D=1.9$ , while it under-predict the TKE after  $x/D=1.9$ . S6WENO5 with  $\phi_{\min}$  of 0.1 performs adversely, at another streamwise position of  $x/D=2.0$ .
- (2) In the wake after the rear cylinder, S6WENO5 schemes with both  $\phi_{\min}$  under-predict the TKE.

The same tendency can be reflected in the two-dimensional TKE fields.

- (1) In the gap region, the high TKE region is presented a little more upstream by C4 schemes with two  $\phi_{\min}$ . The high TKE region by S6WENO5 looks relatively reasonable, but the numerical range of high TKE region looks a little smaller than that of experiment.
- (2) In the region of wake after the rear cylinder, the computations differ from the measurements relatively significant. All the schemes under-predict the TKE.



(a) On the central line in the gap and in the wake



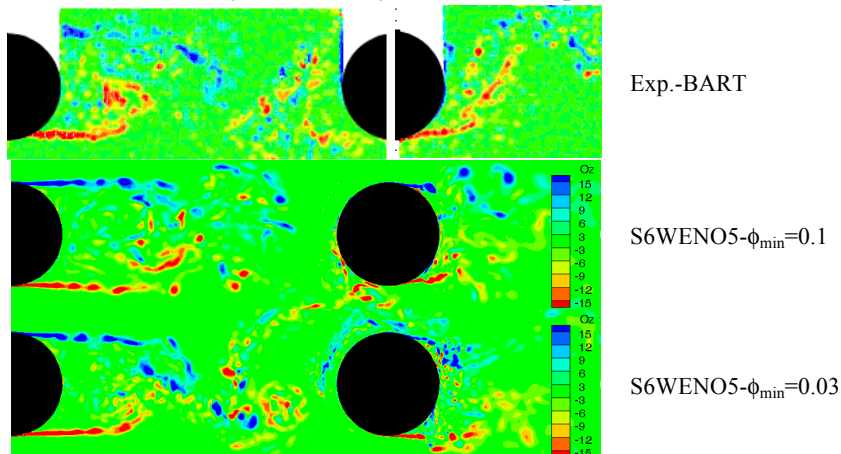
(b) Two-dimensional turbulence flowfields

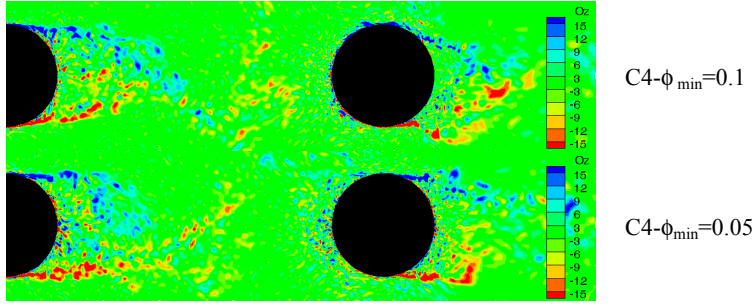
Figure 5 Comparisons of mean TKE

#### 4.2.4 Effects on Instantaneous Spanwise Vorticity and Q Criterion

In the above sub-sections, the mean and root mean square flow quantities by C4 and S6WENO5 with different  $\phi_{\min}$  are compared with the measurements. In this sub-section, the instantaneous flows are presented to demonstrate the performances of the fundamental schemes and different values of  $\phi_{\min}$ . All the numerical schemes coupled with IDDES can resolve the small-scale structures. The primary difference is mainly caused by the fundamental schemes and the  $\phi_{\min}$  has a relatively weak influence on the small motions.

The comparisons of spanwise vorticity are presented in Figure 6. The shear layer instability by C4 scheme seems more upstream and the small-scale structures are smaller than those by S6WENO5 scheme. However, some numerical oscillations are demonstrated by C4 with the two values of  $\phi_{\min}$ . If  $\phi_{\min}$  is smaller, the noise is more obvious. The deficiency of background artificial viscosity ( $k^{(4)}=1/100$ ) is a possible reason, which causes the numerical oscillation. At the same time, the smaller  $\phi_{\min}$  is able to cause the shear layer instability a little more upstream.

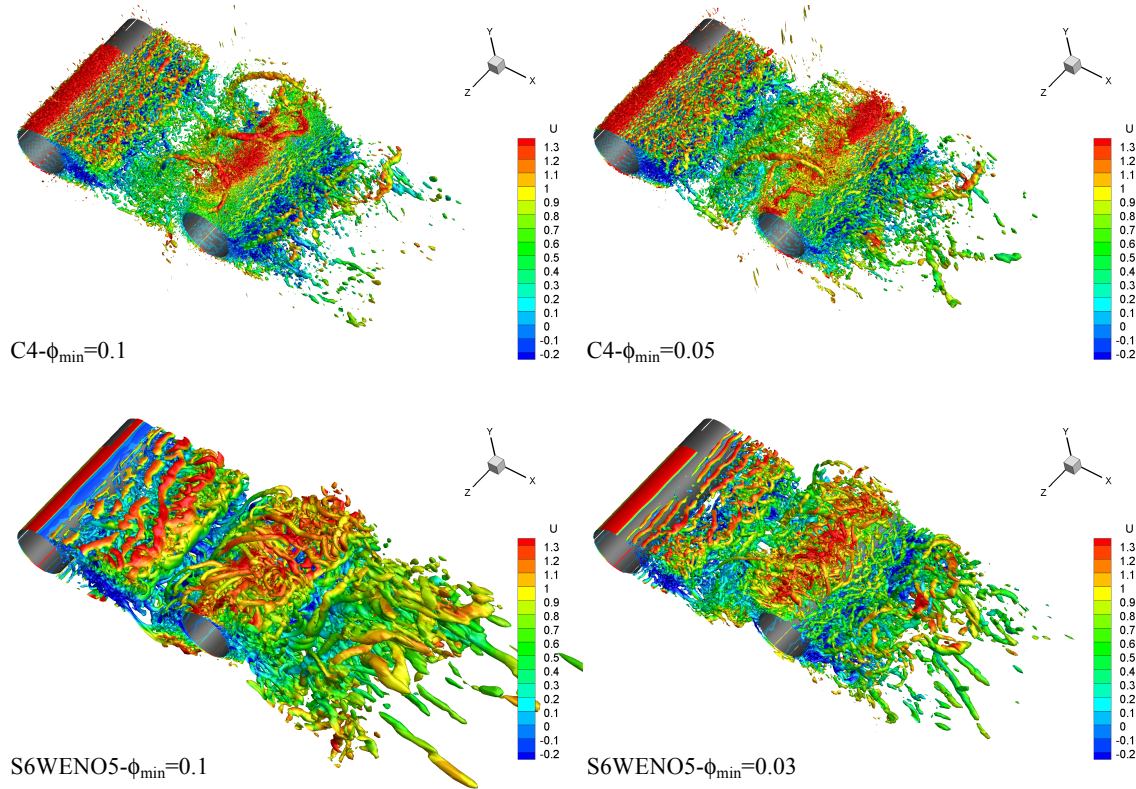




**Figure 6 Comparisons of instantaneous spanwise vorticities**

The comparisons of instantaneous  $Q$  criterion of  $-5$  are demonstrated in Figure 7. All the schemes can well capture the spanwise small-scale structures. Overall, the small-scale structures by C4 scheme are much smaller and more chaotic than those by S6WENO5 scheme.

- (1) On the windward side of the front cylinder, C4 scheme with both  $\phi_{\min}$  present some very small structures near the windward wall. It indicates that the background artificial viscosity is not enough to suppress the numerical noise.
- (2) The performances of both  $\phi_{\min}$  based on S6WENO5 scheme are anticipant, where the freestream is very quiet and small-scale structures are presented in the gap and wake region. The structures by the small  $\phi_{\min}$  of  $0.03$  are more and smaller than those by relatively large  $\phi_{\min}$  of  $0.1$ .



**Figure 7 Comparisons of  $Q$  criterion**

Figure 8 presents the distribution of modeled eddy viscosity and the adaptive function. It is found that the modeled eddy viscosities by C4 and S6WENO5 with different  $\phi_{\min}$  look very similar.

- (1) C4 scheme: The adaptive function by C4 is possibly affected by the grid scale, because the adaptive function  $\phi$  approaches  $\phi_{\min}$ , where the grid scale is small. In addition, the adaptive function  $\phi$  is hoped to be 1 before the front cylinder, where the flow is irrotational. However, an undesired region of adaptive function  $\phi$ , where it is less than 1, is presented. Very small



artificial viscosity before the front cylinder in the irrotational region will lead to the unphysical numerical oscillation in the gap and wake region. The  $\phi_{\min}$  has a weak influence on the modeled eddy viscosity and the distribution of adaptive function.

- (2) S6WENO5 scheme: The distribution of  $\phi$  is anticipant. In the irrotational region,  $\phi$  approaches to 1 to avoid the numerical oscillation. In the separated region,  $\phi$  approaches to  $\phi_{\min}$  to weaken the bad effect of the numerical dissipation on the small-scale motions. However, when is  $\phi_{\min}$  small (0.03), the region of  $\phi_{\min}$  is over-predicted, which even intrudes the irrotational region.

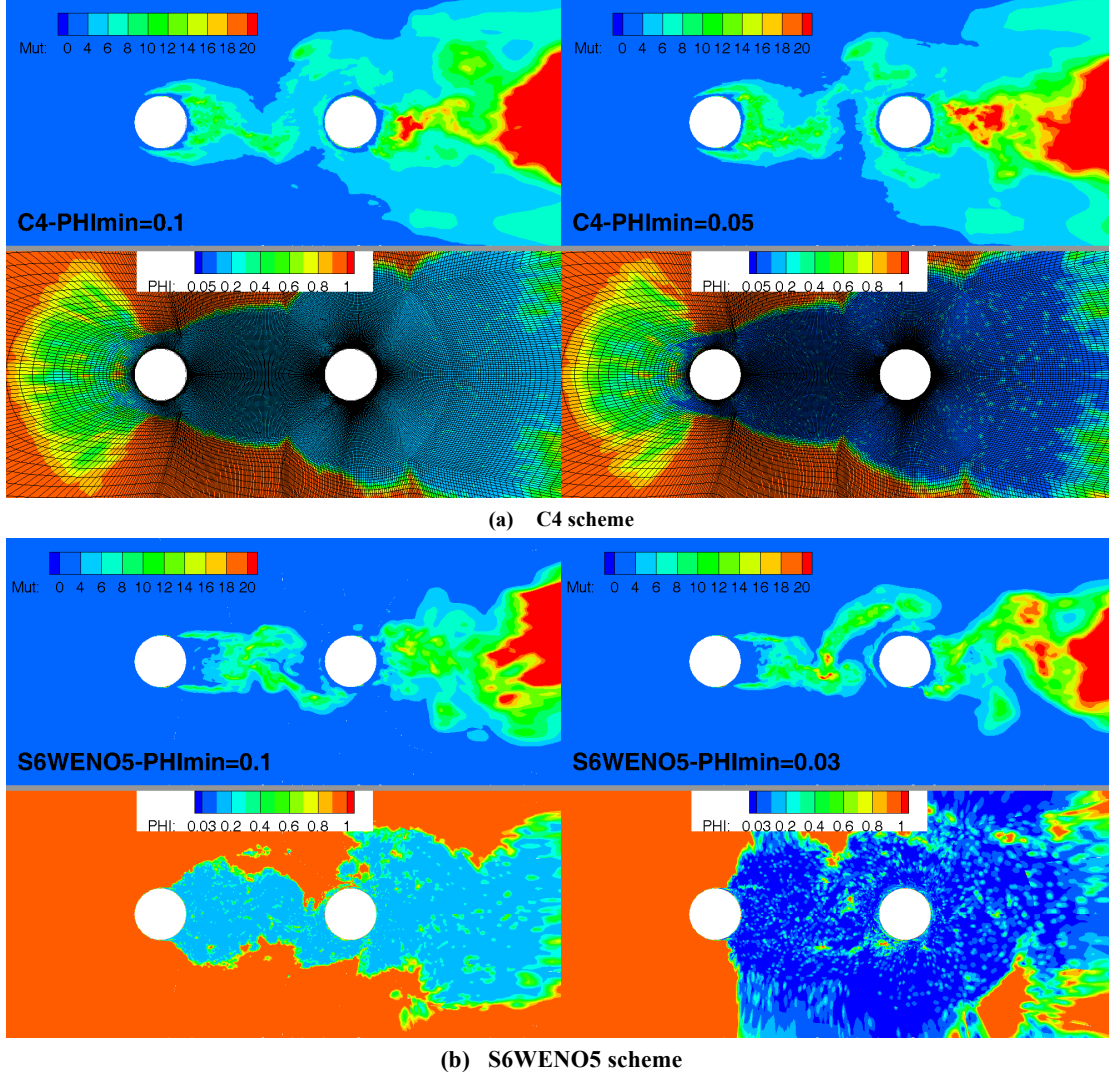


Figure 8 Instantaneous modelled eddy viscosity and adaptive function distributions

## 5 Conclusions and Future Work

The thresholds of adaptive function ( $\phi_{\min}$ ) in the numerical dissipation for C4 and S6WENO5 schemes, coupled with IDDES based on SST model, are evaluated through DHIT and the massively separated flows past the tandem cylinders.

From the DHIT case, the reasonable choices of  $\phi_{\min}$  for C4 and S6WENO4 schemes are recommended after comparing the energy cascade.

After comparing the computations with the available measurements with and without trip, the primary difference of performance is mainly caused by the fundamental schemes, but not  $\phi_{\min}$ . Small  $\phi_{\min}$  always leads to the shear layer instability a little more upstream. S6WENO5 scheme with two values of  $\phi_{\min}$  performs well, and smaller  $\phi_{\min}$  presents more and smaller structures in the gap and wake region.

Due to the insufficient background artificial viscosity, C4 scheme with two values of  $\phi_{\min}$  demonstrates the numerical oscillations in the instantaneous near-fields, although the mean flows by C4 are very similar with those by S6WENO5 scheme.

Large background artificial viscosity of C4 scheme will be investigated to suppress the numerical oscillation before the front cylinder.

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